

**DIAGNOSTIC IN-CLASS QUIZ: DUE FRIDAY OCTOBER 11: GAUSS-JORDAN
ELIMINATION (ORIGINALLY DUE WEDNESDAY OCTOBER 9, BUT POSTPONED)**

MATH 196, SECTION 57 (VIPUL NAIK)

Your name (print clearly in capital letters): _____

PLEASE DO NOT DISCUSS ANY QUESTIONS

The quiz covers basics related to Gauss-Jordan elimination (notes titled **Gauss-Jordan elimination**, corresponding section in the book Section 1.2). Explicitly, the quiz covers:

- Setting up linear systems and interpreting the coefficient matrix in terms of the setup.
- Knowledge of the permissible rules for manipulating linear systems.
- Metacognition of the process of Gauss-Jordan elimination and its eventual result, the reduced row-echelon form, as well as the interpretation in terms of the solution set.

The questions are fairly easy questions if you understand the material. But it's important that you be able to answer them, otherwise what we study later will not make much sense.

- (1) *Do not discuss this!*: The row operations that we can perform on the augmented matrix of a linear system include adding or subtracting another row. However, they do not include multiplying another row. In other words, suppose we start with:

$$\left[\begin{array}{cc|c} 1 & 2 & 5 \\ 2 & 7 & 6 \end{array} \right]$$

What we're not allowed to do is multiply row 2 by row 1 and obtain:

$$\left[\begin{array}{cc|c} 1 & 2 & 5 \\ 2 & 14 & 30 \end{array} \right]$$

What's the most compelling reason for our not being allowed to perform this operation?

- (A) The row operations arise from the corresponding operations on equations. For the "multiplication of rows" operation to be legitimate, it must correspond to multiplication of the corresponding equations, and multiplying equations is not a legitimate operation.
- (B) The row operations arise from the corresponding operations on equations. However, the "multiplication of rows" operation does not correspond to any legitimate operation on equations. Note that it does not correspond to multiplying the equations, because that is not how multiplication of linear polynomials work (in fact, if we multiplied the equations, we would end up with an equation that is not linear).

Your answer: _____

- (2) *Do not discuss this!*: Consider a model where the functional form is linear in the parameters (though not necessarily in the inputs). We can use (input, output) pairs to set up a system of linear equations in the parameters. Given enough such equations, we can determine the values of the parameters.

What is the relation between the coefficient matrix and the parameters and (input, output) pairs?

- (A) The columns of the coefficient matrix correspond to the (input, output) pairs and the rows correspond to the parameters.
- (B) The rows of the coefficient matrix correspond to the (input, output) pairs and the columns correspond to the parameters.

Your answer: _____

- (3) *Do not discuss this!*: Consider a model where the functional form is linear in the parameters (though not necessarily in the inputs). We can use (input, output) pairs to set up a system of linear equations in the parameters. Given enough such equations, we can determine the values of the parameters.

What is the relation between the inputs, the outputs, the coefficient matrix, and the augmenting column?

- (A) The inputs correspond to the coefficient matrix and the outputs correspond to the augmenting column. In other words, knowing the values of the inputs allows us to write down the coefficient matrix. Knowing the values of the outputs allows us to write down the augmenting column.
- (B) The outputs correspond to the coefficient matrix and the inputs correspond to the augmenting column. In other words, knowing the values of the outputs allows us to write down the coefficient matrix. Knowing the values of the inputs allows us to write down the augmenting column.

Your answer: _____

- (4) *Do not discuss this!*: Consider the following rule to check for consistency using the augmented matrix: the system is inconsistent if and only if there is a zero row of the coefficient matrix with a nonzero value for that row in the augmenting column. In what sense does this rule work?

- (A) The rule can be applied to the augmented matrix directly in both the *if* and the *only if* direction.
- (B) The rule can be applied to the augmented matrix only in the *if* direction in general. In the *only if* direction, the rule can be applied to the augmented matrix *after* we have reduced the system to a situation where the coefficient matrix is in row-echelon form (note: it's not necessary to reach reduced row-echelon form).
- (C) The rule can be applied to the augmented matrix only in the *only if* direction in general. In the *if* direction, the rule can be applied to the augmented matrix *after* we have reduced the system to a situation where the coefficient matrix is in row-echelon form (note: it's not necessary to reach reduced row-echelon form).
- (D) The rule can be applied in either direction only *after* we have reduced the system to a situation where the coefficient matrix is in row-echelon form (note: it's not necessary to reach reduced row-echelon form).

Your answer: _____

- (5) *Do not discuss this!*: Which of the following is *not* a possibility for the number of solutions to a system of simultaneous linear equations? Please see Options (D) and (E) before answering.

- (A) 0
- (B) 1
- (C) 2
- (D) All of the above, i.e., none of them is a possibility
- (E) None of the above, i.e., they are all possibilities

Your answer: _____

- (6) *Do not discuss this!*: Which of the following describes the situation for a consistent system of simultaneous linear equations?

- (A) The leading variables are the parameters used to describe the general solution, and the number of leading variables equals the number of nonzero equations in the reduced row-echelon form (here nonzero equation makes an equation that does not have a zero row in the augmented matrix).
- (B) The non-leading variables are the parameters used to describe the general solution, and the number of non-leading variables equals the number of nonzero equations in the reduced row-echelon form (here nonzero equation makes an equation that does not have a zero row in the augmented matrix).
- (C) The leading variables are the parameters used to describe the general solution, and the number of leading variables equals the value (number of variables) - (number of nonzero equations in

the reduced row-echelon form) (here nonzero equation makes an equation that does not have a zero row in the augmented matrix).

- (D) The non-leading variables are the parameters used to describe the general solution, and the number of non-leading variables equals the value (number of variables) - (number of nonzero equations in the reduced row-echelon form) (here nonzero equation makes an equation that does not have a zero row in the augmented matrix).

Your answer: _____